Algebra 2 Honors
WS: Chapter 6 Review

Name $\qquad$
Date $\qquad$ Block $\qquad$

## Part I: Graphing

 Graph each function.1. $f(x)= \begin{cases}2 x-4, & x<0 \\ 5, & x \geq 0\end{cases}$

2. $h(x)=-\frac{4}{3}|x-1|+4$

3. Given $f(x)=2 x^{2}+1$ and $g(x)=f\left(\frac{1}{2} x\right)+1$, graph $g(x)$.

4. $g(x)=\left\{\begin{array}{l}\frac{3}{2} x-1, x \leq 2 \\ \sqrt{x+2}, x>2\end{array}\right.$

5. $k(x)=\left\{\begin{array}{lr}-x, & x \leq-2 \\ -x^{2}-4 x, & x>-2\end{array}\right.$

6. Given $f(x)=2 x-4$ and

$$
g(x)=-\frac{1}{2} f(x)-1, \text { graph } g(x)
$$



## Part II: Problem Solving

7. Given $f(x)=\left\{\begin{array}{l}2 x-2, x \leq 3 \\ -4 x+16, x>3\end{array}\right.$, write the rule for $h(x)$, a vertical translation of $f(x) 2$ units up.
8. Given $f(x)=\left\{\begin{array}{l}3 x+2, x \leq 0 \\ x^{2}\end{array}, x>0\right.$, write the rule for $g(x)$, a horizontal translation of $f(x) 7$ units right.
9. The graph of $f(x)$ is shown below. If $g(x)=-f(x)+1$, what is $g(2)$ ?


Given $f(x)=x^{2}-5 x-14$ and $g(x)=x-7$, find each function.
10. $(f+g)(x)$
11. $(f-g)(x)$
12. $(g-f)(x)$
13. $(f g)(x)$
14. $\left(\frac{f}{g}\right)(x)$
15. $\left(\frac{g}{f}\right)(x)$

Let $f(x)=x-2$ and $g(x)=\frac{8}{x+1}$.
16. Find $f(g(-2))$ and $g(f(-2))$.
17. Find $f(g(1))$ and $g(f(1))$.
18. Find $g(f(x))$ and state its domain.
19. Find $f(g(x))$ and state its domain.

In 20-23, find the inverse of each function. Determine whether the inverse is a function, and state its domain and range.
20. $f(x)=5-8 x$
21. $f(x)=\left(\frac{1}{3} x+2\right)^{2}$
22. $f(x)=\frac{5}{2 x+8}$
23. $f(x)=3+\sqrt{x-5}$

In 24-25, determine by composition whether each pair of functions are inverses.
24. $f(x)=3 x-5$ and $g(x)=\frac{x-3}{5}$
25. $f(x)=\sqrt[3]{x-5}$ and $g(x)=x^{3}+5$
26. The table shows some values for the function $f$. What is the value of $f^{1}(-2)$ ?

| $x$ | -2 | 0 | 2 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 7 | 4 | 1 | -2 |

## Part III: Applications

27. A bicycle delivery service charges $\$ 6$ to deliver a package that weighs 8 ounces or less. For each additional ounce, the services charges $\$ 1.50$ per ounce. Write a piecewise function for the amounts that this company charges to deliver packages that weigh 3 pounds or less.
28. Roscoe earns $\$ 9.50$ per hour at the woodcrafts store for up to 40 hours per week. For each hour over 40 hours, he earns $\$ 13.00$ per hour. Company policy limits his hours to no more than 60 per week. Roscoe wants to know how much he can earn in a week.
(a) Write a piecewise function for earnings $E(h)$ as a function of hours worked (h).
(b) How much will Roscoe earn if he works 56.5 hours in one week?
(c) Roscoe earned $\$ 471$ last week. How many hours did he work?
29. Because of high fuel costs, an airline begins adding fuel surcharge of $\$ 30$ to the price of each airline ticket the airline sells. Also, the airline must add $9 \%$ to the price for airport and sales taxes. Write a composite function for how much a person would pay for a ticket with this airline that is $x$ dollars before surcharges and taxes.
30. The formula for the surface area of a sphere with radius $r$ is $A(r)=4 \pi r^{2}$. Find and interpret the inverse of $A(r)$.
31. The number of times that a cricket chirps per minute can be found by using the function $N(F)=4 F-160$, where $F$ is the temperature in degrees Fahrenheit.
(a) Find and interpret the inverse of $N(F)$.
(b) What is the temperature when the cricket is chirping 60 times a minute?
(c) How many times will the cricket chirp in 1 minute at a temperature of $80^{\circ} \mathrm{F}$ ?
