

## Simplifying Radicals

Simplify. Use absolute value signs when necessary.

1)  $\sqrt{24}$

$2\sqrt{6}$

2)  $\sqrt[3]{1000}$

$10$

3)  $\sqrt[3]{-162}$

$-3\sqrt[3]{6}$

4)  $\sqrt{512}$

$16\sqrt{2}$

5)  $\sqrt[4]{128n^8}$

$2n^2\sqrt[4]{8}$

6)  $\sqrt{98k}$

$7\sqrt{2k}$

7)  $\sqrt[5]{224r^7}$

$2r\sqrt[5]{7r^2}$

8)  $\sqrt[3]{24m^3}$

$2m\sqrt[3]{3}$

9)  $\sqrt{392x^2}$

$14|x|\sqrt{2}$

Disregard absolute value symbols when checking your answers.

10)  $\sqrt{512x^2}$

$16|x|\sqrt{2}$

11)  $\sqrt[4]{405x^3y^2}$

$3\sqrt[4]{5x^3y^2}$

12)  $\sqrt[3]{-16a^3b^8}$

$-2ab^2\sqrt[3]{2b^2}$

13)  $\sqrt[4]{128x^7y^7}$

$2|x| \cdot |y|\sqrt[4]{8x^3y^3}$

14)  $\sqrt[3]{16xy}$

$2\sqrt[3]{2xy}$

15)  $\sqrt[6]{448x^7y^7}$

$2|x| \cdot |y|\sqrt[6]{7xy}$

16)  $\sqrt[3]{56x^5y}$

$2x\sqrt[3]{7x^2y}$

Critical thinking questions:

17) What simplifies into  $2mn^2\sqrt[3]{5mn^2}$  ?

$\sqrt[3]{40m^4n^8}$

18) Simplify  $\sqrt[n]{3 \cdot 2^n \cdot x^{2n} y^{n+3}}$

$2x^2y\sqrt[n]{3y^3}$

## Adding, Subtracting, Multiplying Radicals

**Simplify.**

$$1) -5\sqrt{3} - 3\sqrt{3}$$

$$-8\sqrt{3}$$

$$2) 2\sqrt{8} - \sqrt{8}$$

$$2\sqrt{2}$$

$$3) -4\sqrt{6} - \sqrt{6}$$

$$-5\sqrt{6}$$

$$4) -3\sqrt{5} + 2\sqrt{5}$$

$$-\sqrt{5}$$

$$5) -3\sqrt{27} - 3\sqrt{27} - 3\sqrt{27}$$

$$-27\sqrt{3}$$

$$6) -3\sqrt{12} + 3\sqrt{3} + 3\sqrt{20}$$

$$-3\sqrt{3} + 6\sqrt{5}$$

$$7) -2\sqrt{45} - 3\sqrt{20} - 2\sqrt{6}$$

$$-12\sqrt{5} - 2\sqrt{6}$$

$$8) -3\sqrt[6]{3} - 2\sqrt[6]{192} - \sqrt[6]{320}$$

$$-7\sqrt[6]{3} - 2\sqrt[6]{5}$$

$$9) -3\sqrt[3]{-3} + 2\sqrt[3]{162} + 3\sqrt[3]{81}$$

$$12\sqrt[3]{3} + 6\sqrt[3]{6}$$

$$10) 4\sqrt[6]{3} + 2\sqrt[4]{32} - 3\sqrt[6]{192} - 2\sqrt[6]{192}$$

$$-6\sqrt[6]{3} + 4\sqrt[4]{2}$$

$$11) -\sqrt[3]{320} - 4\sqrt[3]{5} + 2\sqrt[3]{135} + 2\sqrt[3]{16}$$

$$-2\sqrt[3]{5} + 4\sqrt[3]{2}$$

$$12) 2\sqrt[3]{6} - \sqrt[6]{6} + 3\sqrt[3]{6} - 3\sqrt[6]{384}$$

$$5\sqrt[3]{6} - 7\sqrt[6]{6}$$

$$13) \sqrt[3]{3} \cdot \sqrt[3]{-20}$$

$$-\sqrt[3]{60}$$

$$14) \sqrt{5} \cdot \sqrt{3}$$

$$\sqrt{15}$$

$$15) \sqrt{6} \cdot \sqrt{2}$$

$$2\sqrt{3}$$

$$16) \sqrt[3]{3} \cdot \sqrt[3]{9}$$

$$3$$

$$17) 3\sqrt{3}(4 - 3\sqrt{5})$$

$$12\sqrt{3} - 9\sqrt{15}$$

$$18) 4\sqrt{15}(-3\sqrt{6} + 5)$$

$$-36\sqrt{10} + 20\sqrt{15}$$

$$19) 4\sqrt{15}(\sqrt{6} + \sqrt{5})$$

$$12\sqrt{10} + 20\sqrt{3}$$

$$20) -\sqrt{2}(\sqrt{10} - 4\sqrt{6})$$

$$-2\sqrt{5} + 8\sqrt{3}$$

$$21) \sqrt{15}(2\sqrt{10} - 4\sqrt{6})$$

$$10\sqrt{6} - 12\sqrt{10}$$

$$22) (-7 + \sqrt{3x})(4 + \sqrt{3x})$$

$$-28 - 3\sqrt{3x} + 3x$$

$$23) (\sqrt{2a} - 5)(7\sqrt{2a} - 5)$$

$$14a - 40\sqrt{2a} + 25$$

$$24) (2 + \sqrt{5})(-2 + \sqrt{5k})$$

$$-4 + 2\sqrt{5k} - 2\sqrt{5} + 5\sqrt{k}$$

$$25) (\sqrt{3} + \sqrt{5x})(\sqrt{3} - 5\sqrt{5x})$$

$$3 - 4\sqrt{15x} - 25x$$

$$26) (7 + \sqrt{6})(1 + \sqrt{6})$$

$$13 + 8\sqrt{6}$$

## Dividing Radicals

Period \_\_\_\_\_

**Simplify.**

$$1) \frac{\sqrt{9}}{\sqrt{25}}$$

$$\frac{3}{5}$$

$$2) \frac{\sqrt{4}}{\sqrt{36}}$$

$$\frac{1}{3}$$

$$3) \frac{\sqrt{15}}{\sqrt{12}}$$

$$\frac{\sqrt{5}}{2}$$

$$4) \frac{\sqrt{4}}{2\sqrt{20}}$$

$$\frac{\sqrt{5}}{10}$$

$$5) \frac{\sqrt{4}}{4\sqrt{5}}$$

$$\frac{\sqrt{5}}{10}$$

$$6) \frac{4\sqrt{2}}{3\sqrt{5}}$$

$$\frac{4\sqrt{10}}{15}$$

$$7) \frac{-3 - \sqrt{2}}{3\sqrt{17}}$$

$$\frac{-3\sqrt{17} - \sqrt{34}}{51}$$

$$8) \frac{\sqrt{3} + 3\sqrt{5}}{2\sqrt{8}}$$

$$\frac{\sqrt{6} + 3\sqrt{10}}{8}$$

$$9) \frac{\sqrt{3}}{-1 - \sqrt{5}}$$

$$\frac{\sqrt{3} - \sqrt{15}}{4}$$

$$10) \frac{\sqrt{5}}{5 + \sqrt{2}}$$

$$\frac{5\sqrt{5} - \sqrt{10}}{23}$$

$$11) \frac{2 - \sqrt{3}}{-2 - \sqrt{5}}$$

$$4 - 2\sqrt{5} - 2\sqrt{3} + \sqrt{15}$$

$$12) \frac{-4 + \sqrt{3}}{-1 - 2\sqrt{5}}$$

$$\frac{-4 + 8\sqrt{5} + \sqrt{3} - 2\sqrt{15}}{19}$$

$$13) \frac{4 + 3\sqrt{2}}{-3 - \sqrt{5}}$$

$$\frac{-12 + 4\sqrt{5} - 9\sqrt{2} + 3\sqrt{10}}{4}$$

$$14) \frac{3}{-4k^2 - 5\sqrt{k^4}}$$

$$-\frac{1}{3k^2}$$

$$15) \frac{2}{3 - \sqrt{3x^2}}$$

$$\frac{6 + 2x\sqrt{3}}{9 - 3x^2}$$

$$16) \frac{3}{\sqrt{5x} - 3}$$

$$\frac{3\sqrt{5x} + 9}{5x - 9}$$

$$17) \frac{\sqrt[5]{12}}{4\sqrt[5]{-4}}$$

$$-\frac{\sqrt[5]{3}}{4}$$

$$18) \frac{\sqrt[3]{10}}{\sqrt[3]{625}}$$

$$\frac{\sqrt[3]{2}}{5}$$

$$19) \frac{\sqrt[5]{2}}{3\sqrt[5]{162}}$$

$$\frac{\sqrt[5]{3}}{9}$$

$$20) \frac{3\sqrt[4]{4}}{2\sqrt[4]{8}}$$

$$\frac{3\sqrt[4]{8}}{4}$$

$$21) \frac{\sqrt[4]{5}}{4\sqrt[4]{27}}$$

$$\frac{\sqrt[4]{15}}{12}$$

$$22) \frac{\sqrt[3]{10}}{\sqrt[3]{32}}$$

$$\frac{\sqrt[3]{20}}{4}$$

$$23) \frac{-5 + 5\sqrt[4]{5}}{3\sqrt[4]{6}}$$

$$\frac{-5\sqrt[4]{216} + 5\sqrt[4]{1080}}{18}$$

$$24) \frac{3 + \sqrt[3]{3}}{\sqrt[3]{9}}$$

$$\frac{3\sqrt[3]{3} + \sqrt[3]{9}}{3}$$

$$25) \frac{-2x + \sqrt[3]{-5x^4y^3}}{3\sqrt[3]{15x^3y}}$$

$$\frac{-2\sqrt[3]{225y^2} - 5y\sqrt[3]{9y^2x}}{45y}$$

$$26) \frac{3 - \sqrt[4]{5k^2}}{\sqrt[4]{3k^3}}$$

$$\frac{3\sqrt[4]{27k} - \sqrt[4]{135k^3}}{3k}$$