

14.1 Sequences, Series and Summation (S^3)

Let's look at the following lists of numbers, often called _____.

1, 3, 5, 7, 9, 11, ...

$$a_1 = \underline{\hspace{2cm}}$$

$$a_2 = \underline{\hspace{2cm}}$$

$$a_{13} = \underline{\hspace{2cm}}$$

$$a_n = \underline{\hspace{2cm}}$$

Converge or Diverge?

$0, \frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}, \dots$

$$a_1 = \underline{\hspace{2cm}}$$

$$a_2 = \underline{\hspace{2cm}}$$

$$a_{54} = \underline{\hspace{2cm}}$$

$$a_n = \underline{\hspace{2cm}}$$

Converge or Diverge?

$$a_1 = \underline{\hspace{2cm}}$$

$$a_2 = \underline{\hspace{2cm}}$$

$$a_{100} = \underline{\hspace{2cm}}$$

$$a_n = (-3)^n$$

Converge or Diverge?

You try!

6, 8, 10, 12, 14 ...

$$a_1 = \underline{\hspace{2cm}}$$

$$a_2 = \underline{\hspace{2cm}}$$

$$a_{19} = \underline{\hspace{2cm}}$$

$$a_n = \underline{\hspace{2cm}}$$

Converge or Diverge?

$$a_1 = \underline{\hspace{2cm}}$$

$$a_2 = \underline{\hspace{2cm}}$$

$$a_{44} = \underline{\hspace{2cm}}$$

$$a_n = (-1)^{(n+1)}$$

Converge or Diverge?

-100, 10, -1, 0.1, -0.01, ...

$$a_1 = \underline{\hspace{2cm}}$$

$$a_2 = \underline{\hspace{2cm}}$$

$$a_9 = \underline{\hspace{2cm}}$$

$$a_n = \underline{\hspace{2cm}}$$

Converge or Diverge?

Sometimes, we define sequences based on a formula using previous terms. These formulas are called _____.

Example: Find the first four terms of the sequence using the recursive formula that is given:

$$1. \quad \begin{aligned} a_n &= 4a_{n-1} - 3 \\ a_1 &= 2 \end{aligned}$$

$$2. \quad \begin{aligned} a_n &= \frac{1}{2}a_{n-1} \\ a_1 &= 16 \end{aligned}$$

You try!

$$3. \quad \begin{aligned} a_n &= n * a_{n-1} \\ a_1 &= 1 \end{aligned}$$

A _____ is the sum of all of the terms of a sequence. So the

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Write your questions and thoughts here!



So the sequence 12, 15, 18, 21 would have the corresponding series of _____.

To help us write series compactly, we use _____.

$$\sum_{k=1}^n a_k$$

Example: Rewrite each series as a sum.

You try!

4. $\sum_{n=0}^5 4n$

5. $\sum_{p=1}^4 p^p$

6. $\sum_{m=7}^{10} m(m+3)$

Example: Evaluate each series.

You try!

7. $\sum_{n=0}^4 3^n$

8. $\sum_{h=1}^4 (-1)^{(h-1)} \frac{1}{h}$

9. $\sum_{k=4}^7 \frac{k^2}{2}$

Example: Rewrite the series using sigma notation with $k = 0$ and $k = 1$.

You try!

10. $1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6}$

11. $1 - \frac{2}{3} + \frac{4}{9} - \frac{8}{27} + \frac{16}{81}$

Calculator? Mode: Change "Function to Sequence"



Now summarize what you learned!

14.1 Practice

Find the next three terms in each sequence. Then, tell if the sequence converges or diverges.

1) 2, 6, 18, 54, 162, ...

2) -1, 2, 7, 14, 23, ...

3) -3, 15, -75, 375, -1875, ...

4) 1, 1.1, 1.11, 1.111, ...

Find the first four terms in each sequence, given the explicit formula.

5) $a_n = 5^{n-1}$

6) $a_n = -12 + 30n$

7) $a_n = n^2 - 1$

8) $a_n = \frac{8}{n+2}$

Find the first four terms in each sequence, given the recursive formula.

9) $a_n = a_{n-1} + \frac{3}{2}$
 $a_1 = 0$

10) $a_n = a_{n-1} \cdot -5$
 $a_1 = -3$

11) $a_n = a_{n-1} \cdot 4$
 $a_1 = 3$

12) $a_n = \frac{2 + a_{n-1}}{2}$
 $a_1 = 10$

Write the explicit formula for each sequence.

13) 4, 20, 100, 500, 2500, ...

14) 29, 20, 11, 2, -7, ...

15) $1, \frac{3}{2}, 2, \frac{5}{2}, 3, \dots$

16) $2, 5, 10, 17, 26, \dots$

Write the recursive formula for each sequence.

17) $3, -6, 12, -24, 48, \dots$

18) $-3, -\frac{3}{4}, -\frac{3}{16}, -\frac{3}{64}, -\frac{3}{256}, \dots$

19) $-4, -8, -16, -32, -64, \dots$

20) $3, -\frac{3}{5}, \frac{3}{25}, -\frac{3}{125}, \frac{3}{625}, \dots$

Evaluate each series.

21) $\sum_{k=1}^6 (3k^2 - 2)$

22) $\sum_{a=2}^8 (20 - a)$

23) $\sum_{k=1}^6 k(k - 2)$

24) $\sum_{k=4}^9 k^2$

25) $\sum_{m=5}^{11} (40 - m)$

26) $\sum_{k=0}^4 (3k^2 + 3)$

Rewrite each series using sigma notation.

27) $4 + 16 + 64 + 256$

28) $1 + 4 + 9 + 16 + 25$

29) $301 + 302 + 303 + 304 + 305 + 306$

30) $601 + 602 + 603 + 604$