

## Warm Up

Complete the table summarizing the notes on 5.1 Variation Functions

Type of Variation	Equation that describes relationship
y varies directly as x	$y = kx$
y varies inversely as x	$y = \frac{k}{x}$
y varies jointly as x and z	$y = kxz$
y varies inversely as x and directly as z	$y = \frac{kz}{x}$

1. The volume  $V$  of a pyramid varies jointly as the area of the base  $B$  and the height  $h$ , and  $V = 24 \text{ ft}^3$  when  $B = 12 \text{ ft}^2$  and  $h = 6 \text{ ft}$ . Find  $B$  when  $V = 54 \text{ ft}^3$  and  $h = 9 \text{ ft}$ .

$$18 \text{ ft}^2$$

2. The cost per person  $c$  of chartering a tour bus varies inversely as the number of passengers  $n$ . If it costs \$22.50 per person to charter a bus for 20 passengers, how much will it cost per person to charter a bus for 36 passengers?

$$\$12.50$$

3. The pressure  $P$  of a gas varies inversely as its volume  $V$  and directly as the temperature  $T$ . A certain gas has a pressure of 2.7 atm, a volume of 3.6 L, and a temperature of 324 K. If the volume of the gas is kept constant and the temperature is increased to 396 K, what will the new pressure be?

$$3.3 \text{ atm}$$

③

$$P = \frac{KT}{V}$$

$$3.6 \cdot 2.7 = \frac{K(324)}{3.6} \quad \leftarrow 3.6$$

$$9.72 = \frac{324K}{324}$$

$$K = 0.03$$

$$P = \frac{0.03(396)}{3.6}$$

$$K = \frac{PV}{T}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{2.7(3.6)}{324} = \frac{P(3.6)}{396}$$

$$39. \quad y = kxz$$

$$I = kdt$$

$$12.50 = 2500 \cdot \frac{1}{4} \cdot k$$

$$k = 0.02$$

$$y = kxz^2$$

$$\frac{y_1}{x_1 z_1^2} = \frac{y_2}{x_2 z_2^2}$$

$$\frac{189}{7(9^2)} = \frac{y}{2(6^2)}$$

## 5.2 Multiplying & Dividing Rational Expressions

A rational expression is a quotient of two polynomials.

Before we can multiply and divide rational expressions, let's first see how we simplify rational expressions.

### Simplifying Rational Expressions

To simplify a rational expression, divide out common factors that appear in the numerator and denominator. Because you're looking for common factors, always remember to **FACTOR FIRST!!** Also make note of when the expression is undefined.

### Caution!

When identifying values for which a rational expression is undefined, identify the values of the variable that make the original denominator equal to 0.

Examples: Simplify. Identify any values for which the expression is undefined.

(1) *When does the denom = 0?*

$$\frac{x^2 - 4x - 12}{x^2 - 4} = \frac{(x-6)(x+2)}{(x+2)(x-2)}$$

(2)  $\frac{x^2 - 4}{x^2 - 4} = \frac{(x-6)(x-2)}{(x-2)(x-2)}$ , undefined when  $x=2$  or  $x=-2$

(3)  $\frac{3x + 4}{3x^2 + x - 4} = \frac{\cancel{(3x+4)}}{\cancel{(3x+4)}(x-1)} = \frac{1}{x-1}$   
 undefined when  $x=1, -\frac{4}{3}$

(4)  $\frac{4x - x^2}{x^2 - 2x - 8} = \frac{x(4-x)}{(x-4)(x+2)} = \frac{-x(x-4)}{\cancel{(x-4)}(x+2)}$   
 undefined when  $x=-2$

Multiplying Rational Expressions

- factor all numerators and denominators completely
- simplify as you go by dividing out common factors of the numerators and denominators
- multiply ACROSS
- leave answers in factored form

Examples

Assume that all expressions are defined.

$$(1) \frac{n^5}{n-6} \cdot \frac{n^2-6n}{n^8} = \frac{\cancel{n}^5}{\cancel{n}^1 \cancel{6}} \cdot \frac{n(n\cancel{6})}{\cancel{n}^8 \cancel{n}^3} = \frac{1}{n^2}$$

$$(2) \frac{x^2-5x-24}{6x+2x^2} \cdot \frac{5x^2}{x-8} = \frac{\cancel{(x-8)}\cancel{(x+3)}}{2x(3+x)} \cdot \frac{5x^2}{\cancel{(x-8)}} = \frac{5x^2}{2x} = \frac{5x}{2}$$

$$(3) \frac{40-10x}{x^2-6x+8} \cdot \frac{x+3}{5x+15}$$

$$\frac{-10(4-x)}{\cancel{(x-4)}(x-2)} \cdot \frac{\cancel{(x+3)}}{5(x+3)} = \frac{-10}{5(x-2)} = \frac{-2}{x-2}$$

Dividing Rational Expressions

- rewrite problem as a multiplication problem

"keep-change-flip"

Examples

Assume that all expressions are defined.

$$(1) \frac{x+2}{x+3} \div \frac{x^2+x-12}{x^2-9}$$

$$\frac{(x+2)}{\cancel{(x+3)}} \cdot \frac{\cancel{(x-3)}\cancel{(x+3)}}{(x+4)(x-3)} = \frac{x+2}{x+4}$$

$$(2) \frac{3x+6}{x^2-9} \div \frac{6x^2+12x}{4x+12}$$

$$(3) \frac{2x^2-7x-4}{x^2-9} \div \frac{4x^2-1}{8x^2-28x+12} = \frac{4(x-4)}{x+3}$$