

Warm Up

Factor the expression *completely*.

1.  $25z^2 - y^2$

2.  $25x^2 - 1$

3.  $49x^2 + 28xy + 4y^2$

4.  $\frac{1}{x^2} - 1$

5.  $8y^2 - 2$

6.  $4rs^2 - 4rs + r$

Review

Solve the equation using square roots.

1.  $x^2 + 4x + 4 = 36$

2.  $x^2 - 6x + 9 = 1$

3.  $x^2 - 22x + 121 = 81$

Core Concept

Completing the Square

Words: \_\_\_\_\_

Algebra: \_\_\_\_\_

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**Example #1**

Find the value of  $c$  that makes  $x^2 + 14x + c$  a perfect square trinomial. Then write the expression as the square of a binomial.

(a)  $x^2 + 8x + c$

(b)  $x^2 - 2x + c$

(c)  $x^2 - 9x + c$

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**Example #2**

Solve  $x^2 - 10x + 7 = 0$  by completing the square.

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**Example #3**

Solve  $3x^2 + 12x + 15 = 0$  by completing the square.

### Additional Practice

Solve the equation by completing the square.

(a)  $x^2 - 4x + 8 = 0$

(b)  $x^2 + 8x - 5 = 0$

(c)  $-3x^2 - 18x - 6 = 0$

(d)  $4x^2 + 32x = -68$

(e)  $6x(x + 2) = -42$

(f)  $2x(x - 2) = 200$

### Example #4

Write  $y = x^2 - 12x + 18$  in vertex form. Then identify the vertex.

Write the quadratic function in vertex form. Then identify the vertex.

(a)  $y = x^2 - 8x + 18$

(b)  $y = x^2 + 6x + 4$

(c)  $y = x^2 - 2x - 6$

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**Example #5**

The height  $y$  (in feet) of a baseball  $t$  seconds after it is hit can be modeled by the function  $y = -16t^2 + 96t + 3$ . Find the maximum height of the baseball. How long does the ball take to hit the ground?

**WHAT IF?** The height of the baseball can be modeled by  $y = -16t^2 + 80t + 2$ . Find the maximum height of the baseball. How long does the ball take to hit the ground?