

\*Work attached

All work and answers should be done on separate paper. Make sure your work is legible and all steps involved can be clearly followed.

In 1 - 5, simplify completely.

$$1. \frac{\sin\left[\left(\frac{\pi}{2}\right) - x\right]}{\cos\left[\left(\frac{\pi}{2}\right) - x\right]} = \cot x$$

$$4. \cot x \sec x = \csc x$$

$$2. (1 - \cos^2 x)(\csc x) = \sin x$$

$$5. \cos^2 x (\sec^2 x - 1) = \sin^2 x$$

$$3. \frac{\sin(-x)}{\cos(-x)} = -\tan x$$

In 6 - 9, verify the identity.

$$6. (\tan^2 x + 1)(\cos^2 x - 1) = -\tan^2 x$$

$$7. \frac{\cos x}{1 - \sin x} = \sec x + \tan x$$

Work may vary

$$8. \csc^4 x - 2 \csc^2 x + 1 = \cot^4 x$$

$$9. \frac{\tan x}{\csc x} + \frac{\sin x}{\tan x} = \sec x$$

In 10 - 13, find the general solutions to each equation.

$$10. 2 \cos x + \sqrt{2} = 0 \quad x = \frac{3\pi}{4} + 2n\pi, \frac{5\pi}{4} + 2n\pi$$

$$11. 4 \sin^2 x - 3 = 0 \quad x = \frac{\pi}{3} + 2n\pi, \frac{2\pi}{3} + 2n\pi, \frac{4\pi}{3} + 2n\pi, \frac{5\pi}{3} + 2n\pi$$

$$12. 2 \sin^2 x - 3 \sin x + 1 = 0 \quad x = \frac{\pi}{6} + 2n\pi, \frac{5\pi}{6} + 2n\pi, \frac{\pi}{2} + 2n\pi$$

$$13. \sec^2 x - \tan x = 1 \quad x = n\pi, \frac{\pi}{4} + n\pi$$

In 14 - 15, find all solutions on the interval  $[0, 2\pi)$ . When necessary, round decimals to the nearest thousandth.

$$14. 4 \sin 3x = 2\sqrt{3} \quad x = \left\{ \frac{\pi}{9}, \frac{7\pi}{9}, \frac{13\pi}{9}, \frac{2\pi}{9}, \frac{8\pi}{9}, \frac{14\pi}{9} \right\}$$

$$15. 5 \tan^2 x + 8 \tan x - 4 = 0 \quad x = \{0.381, 3.522, 2.034, 5.176\}$$

$$\textcircled{1} \frac{\sin\left[\frac{\pi}{2}-x\right]}{\cos\left[\frac{\pi}{2}-x\right]} = \frac{\cos x}{\sin x} = \text{cot } x$$

$$\textcircled{2} (1-\cos^2 x)(\csc x) = \sin^2 x \left(\frac{1}{\sin x}\right) = \sin x$$

$$\textcircled{3} \frac{\sin(-x)}{\cos(-x)} = \frac{-\sin x}{\cos x} = -\tan x$$

$$\textcircled{4} \cot x \sec x = \frac{\cos x}{\sin x} \cdot \frac{1}{\cos x} = \csc x$$

$$\textcircled{5} \cos^2 x (\sec^2 x - 1) = \cos^2 x \cdot \tan^2 x = \cos^2 x \cdot \frac{\sin^2 x}{\cos^2 x} = \sin^2 x$$

$$\textcircled{6} \begin{aligned} (\tan^2 x + 1)(\cos^2 x - 1) &= -\tan^2 x \\ \sec^2 x (-\sin^2 x) &= \\ \frac{1}{\cos^2 x} \cdot -\sin^2 x &= \\ -\tan^2 x &= -\tan^2 x \checkmark \end{aligned}$$

$$\textcircled{7} \frac{\cos x}{1-\sin x} = \sec x + \tan x$$

$$\frac{\cos x (1+\sin x)}{(1-\sin x)(1+\sin x)} =$$

$$\frac{\cos x (1+\sin x)}{(1-\sin^2 x)} =$$

$$\frac{\cos x (1+\sin x)}{\cos^2 x} =$$

$$\frac{1}{\cos x} + \frac{\sin x}{\cos x} =$$

$$\sec x + \tan x = \sec x + \tan x \checkmark$$

$$\textcircled{8} \begin{aligned} \csc^4 x - 2\csc^2 x + 1 &= \cot^4 x \\ (\csc^2 x - 1)(\csc^2 x - 1) &= \\ (\cot^2 x)(\cot^2 x) &= \\ \cot^4 x &= \cot^4 x \checkmark \end{aligned}$$

$$\textcircled{9} \quad \frac{\tan x}{\csc x} + \frac{\sin x}{\tan x} = \sec x$$

$$\frac{\tan^2 x + \csc x \sin x}{\csc x \tan x} =$$

$$\frac{\tan^2 x + 1}{\csc x \tan x} =$$

$$\frac{\sec^2 x}{\frac{1}{\sin x} \cdot \frac{\sin x}{\cos x}} =$$

$$\frac{\sec^2 x}{\sec x} =$$

$$\sec x = \sec x \checkmark$$

$$\textcircled{10} \quad 2 \cos x + \sqrt{2} = 0$$

$$\cos x = -\frac{\sqrt{2}}{2}$$

$$x = \frac{3\pi}{4} + 2n\pi, \frac{5\pi}{4} + 2n\pi$$

$$\textcircled{11} \quad 4 \sin^2 x - 3 = 0$$

$$\sin^2 x = \frac{3}{4}$$

$$\sin x = \pm \frac{\sqrt{3}}{2}$$

$$x = \frac{\pi}{3} + 2n\pi, \frac{2\pi}{3} + 2n\pi, \frac{4\pi}{3} + 2n\pi, \frac{5\pi}{3} + 2n\pi$$

OR

$$\frac{\pi}{3} + n\pi, \frac{2\pi}{3} + n\pi$$

$$\textcircled{12} \quad 2\sin^2 x - 3\sin x + 1 = 0$$

$$(2\sin x - 1)(\sin x - 1) = 0$$

$$\sin x = 1/2 \quad \sin x = 1$$

$$x = \frac{\pi}{6} + 2n\pi, \frac{5\pi}{6} + 2n\pi, \frac{\pi}{2} + 2n\pi$$

$$\textcircled{13} \quad \sec^2 x - \tan x = 1$$

$$1 + \tan^2 x - \tan x = 1$$

$$\tan x = 0 \quad \tan x = 1$$

$$\tan^2 x - \tan x = 0$$

$$x = 0 + n\pi, \frac{\pi}{4} + n\pi$$

$$\tan x (\tan x - 1) = 0$$

$$\textcircled{14} \quad 4\sin 3x = 2\sqrt{3}$$

$$\sin 3x = \frac{\sqrt{3}}{2}$$

$$\left\{ \frac{\pi}{9}, \frac{7\pi}{9}, \frac{13\pi}{9}, \frac{2\pi}{9}, \frac{8\pi}{9}, \frac{14\pi}{9} \right\}$$

$$3x = \frac{\pi}{3} + 2n\pi, \frac{2\pi}{3} + 2n\pi$$

$$x = \frac{\pi}{9} + \frac{2n\pi}{3}, \frac{2\pi}{9} + \frac{2n\pi}{3}$$

$$\textcircled{15} \quad 5\tan^2 x + 8\tan x - 4 = 0$$

$$(5\tan x - 2)(\tan x + 2) = 0$$

$$\tan x = 2/5 \quad \tan x = -2$$

$$x = 0.381 + n\pi$$

$$x = 2.034 + n\pi$$

$$x = \{0.381, 3.522, 2.034, 5.176\}$$