

[8.3: SOLVING SYSTEMS BY ELIMINATION] 1

Write your questions here!

We have learned how to solve linear systems by graphing and substitution. Now we will learn how to solve the linear systems by using a method called **elimination**.

Steps for Solving Linear Systems by Elimination

- Step 1 • Make sure that all of the variables and the equal sign are "lined up."
- Step 2 • Decide which coefficients you want to cancel out. To cancel out, they must be opposites. You might have to multiply the equations first!
- Step 3 • Add the two equations and solve new equation. (One variable should cancel out!)
- Step 4 • Take your answer to Step 3 and substitute it into either of the original equations.
- Step 5 • Write your solution as a coordinate point or as a pair of values.

Example 1: Solve the linear system using elimination:

$$3x - 4y = 10$$

$$5x + 4y = 6$$

Step 1: Do you have x over x, y over y and equal sign over equal sign? Yup!

Continue on...

Step 2: The y's are already opposites. Our work here is done.

Step 3: Add the two equations. Solve the resulting equation.

Step 4: Take the answer from **Step 3** and plug it into either of the original equations and solve for the other unknown variable.

Step 5: Write your solution as a coordinate point or as a pair of values.

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Write your questions here!

More Examples:

2. $2x - y = 12$
 $-2x - 3y = -12$

3. $x + 2y = 4$
 $-6x + 2y = -10$

4. $4x - 3y = 8$
 $2x - 2y = 0$

5. $9x + 2y = 39$
 $6x + 13y = -9$

Now, summarize
your notes here!

Practice 8.3 Systems of Equations (Elimination)

Show all of your work!

Solve each system by elimination.

1) $-4x - 4y = 8$
 $-x + 4y = 12$

2) $3x + 2y = -3$
 $-3x + y = 12$

3) $x - 2y = -9$
 $-4x - 2y = -4$

4) $-2x + y = 4$
 $-2x + 2y = 0$

5) $-4x - y = 8$
 $-12x + 3y = -24$

6) $-x + 4y = -1$
 $-2x - 8y = 14$

$$\begin{aligned} 7) \quad & -6x + 3y = 3 \\ & 5x - 8y = -8 \end{aligned}$$

$$\begin{aligned} 8) \quad & 4x - 3y = -16 \\ & 5x + 2y = 3 \end{aligned}$$

$$\begin{aligned} 9) \quad & 3x + 2y = 10 \\ & 4x + 5y = 18 \end{aligned}$$

$$\begin{aligned} 10) \quad & -5x - 6y = -3 \\ & 2x + 4y = 6 \end{aligned}$$

11) Is the point $(0, 0)$ a solution of the system of linear equations below?

$$\begin{aligned} 2x + y &= 2 \\ 4x - 2y &= 2 \end{aligned}$$

12) Is the point $(\frac{5}{4}, 7)$ a solution of the system of linear equations below?

$$\begin{aligned} 4x + y &= 12 \\ -4x + 3y &= 16 \end{aligned}$$

Application and Extension

$$\begin{aligned}2x + 2y &= 2 \\ -8x + 4y &= 16\end{aligned}$$

1. Solve the following system of equations using elimination.
2. You have just enough coins to pay for a loaf of bread priced at \$1.95. You know you have a total of 12 coins, with only quarters and dimes. Let Q = the number of quarters and D = the number of dimes. Complete:

$$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} = 12 \quad \text{Representing the number of coins.}$$

$$0.10 \underline{\hspace{2cm}} + 0.25 \underline{\hspace{2cm}} = \$1.95 \quad \text{Representing the value of the coins.}$$

Now, solve the linear system using elimination.

(Hint: Multiply the second equation by -10!)

3. The table shows the number of apples needed to make apple pies and applesauce sold at a farm store. During a recent picking at the farm, 169 Granny Smith apples and 95 Red Delicious apples were picked. Write and solve a system to determine how many apple pies and how many batches of applesauce can be made if every apple is used. *(Hint: read across each row to create your equations!)*

Type of Apple	# Needed for π (Pie)	# Needed for Sauce	Total
Granny Smith	5	4	169
Red Delicious	3	2	95

3. The Algebros are visting Michigan State University when they stumble upon a Girl Scout selling cookies. Sully orders 3 boxes of Tagalongs and 4 boxes of Somoas for \$26. Brust isn't statisfied with such a small order and yells "**UPGRADE!!**" He then upgrades the order to 5 boxes of Tagalongs and 6 Boxes of Somoas which costs \$41.

a. Write a system of linear equations to model the situation.
(Let x = cost of a box of Tagalongs and y = cost of a box of Somoas.)

b. Solve your system of equations above using elimination to find the cost of each type of cookie.