

[8.2: SOLVING SYSTEMS BY SUBSTITUTION] 1

Write your questions here!

We have learned how to solve linear systems by graphing. Now we will learn how to solve the linear systems by using a method called .

Steps for Solving Linear Systems by Substitution

- Step 1 • Solve one of the equations for one of its variables. When possible, solve for a variable that has a coefficient of 1.
- Step 2 • Substitute the expression from Step 1 into the other equation and solve for the other variable.
- Step 3 • Substitute the value from Step 2 into either original equation and solve for the remaining variable.
- Step 4 • Write your solution as a coordinate point or as a pair of values.

Example 1: Solve the linear system using substitution:

$$\begin{aligned}4x + 6y &= 4 \\ x &= -6 + 2y\end{aligned}$$

Step 1: Solve one of the equations for one of its variables.

Step 2: Now, substitute the expression from **Step 1** into the OTHER equation and solve.

Step 3: Next, substitute the value from **Step 2** into either of the original equations and solve for the last unknown variable.

Step 4: Write your solution as a coordinate point or as a pair of values.

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Write your questions here!



More Examples:

2. $y = -7 - 3x$
 $-2x + 4y = 0$

3. $x = 2y + 5$
 $x = 10 - 3y$

4. $x - 1 = y$
 $2x - y = 5$

5. $x - y = 3$
 $2x - y = 5$

Now, summarize
your notes here!



Practice 8.2 Systems of Equations (Substitution)

Show all of your work!

Solve each system by substitution.

1) $4x - 4y = -4$
 $y = -4x + 1$

2) $y = 2x - 7$
 $2x - 4y = 10$

3) $8x + 5y = -24$
 $y = 5x + 15$

4) $y = -4x - 5$
 $6x - 5y = -1$

5) $y = 4x - 24$
 $-3x - 5y = -18$

6) $y = 4x - 17$
 $4x + 4y = 12$

7) $x = -1 - 3y$
 $2x - 4y = -22$

8) $-x + 3y = 4$
 $x = 4y - 3$

9) $4x + y = -3$
 $-7x - 3y = 9$

10) $x = 5y - 11$
 $-9x - 7y = -5$

11) Is the point $(-1, 3)$ a solution of the system of linear equations below?

$$\begin{aligned}x + y &= 2 \\ y - x &= 2\end{aligned}$$

12) Is the point $(1, 7)$ a solution of the system of linear equations below?

$$\begin{aligned}2x - 4 &= 5 \\ x &= 1\end{aligned}$$

Application and Extension

1. Solve the following system of equations using substitution. Write your answers as fractions, if necessary.

$$\begin{aligned} -x + 2y &= -2 \\ y &= 3x + 4 \end{aligned}$$

2. In the March 1998 issue of **Great Goatee Magazine**, readers could vote online for their favorite goatee in the *Pitt-Brust Bonanza*. Readers could either vote for Brad Pitt or Mr. Brust. Brust's votes equaled 2 times the sum of Pitt's votes and 400. The total number of votes received was 2012.

a. Model the situation with a linear system.



Pitt?

Let B = # vote for Brust
Let P = # votes for Pitt

Total # of votes: _____ + _____ = 2012

Brust vs Pitt: _____ = 2 (_____ + _____)



Brust?

b. Now solve your system using substitution. By how many votes did Brust win the contest?

c. Explain why solving this by graphing wouldn't be ideal.